

GAUSS MAPS OF THE SURFACES IN THE THREE-DIMENSIONAL HEISENBERG GROUP

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Abstract. In this paper we study the Gauss map of surfaces in three-dimensional Heisenberg group using the Gans model of the hyperbolic plane. We establish a relationship between the tension fields of the Gauss maps and the mean curvatures of the surfaces in \mathcal{H}_3 .

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Keywords: Gauss map, Heisenberg group, mean curvature, tension field

Contents

1	Introduction	2
2	The Gans Model	2
2.1	Isometries	3
2.2	Geodesics	4
3	The Geometry of the Heisenberg Group	4
4	Surfaces in \mathcal{H}_3	6
4.1	Graph over the XOY-Plane	6
4.2	Vertical Surface	7
5	The Gauss Map	8
6	Tension Field and Mean Curvature of Surfaces in \mathcal{H}_3	11
6.1	Minimal Graphs of Rank One	14
6.2	Minimal Graphs of Rank Two	15
7	Conclusions	16
	Appendix: Tension Field	16
	References	22