



## MODULAR FORMS ON BALL QUOTIENTS OF NON-POSITIVE KODAIRA DIMENSION\*

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**Abstract.** The Baily-Borel compactification  $\widehat{\mathbb{B}/\Gamma}$  of an arithmetic ball quotient admits projective embeddings by  $\Gamma$ -modular forms of sufficiently large weight. We are interested in the target and the rank of the projective map  $\Phi$ , determined by  $\Gamma$ -modular forms of weight one. This paper concentrates on the finite  $H$ -Galois quotients  $\mathbb{B}/\Gamma_H$  of a specific  $\mathbb{B}/\Gamma_{-1}^{(6,8)}$ , birational to an abelian surface  $A_{-1}$ . Any compactification of  $\mathbb{B}/\Gamma_H$  has non-positive Kodaira dimension. The rational maps  $\Phi^H$  of  $\widehat{\mathbb{B}/\Gamma_H}$  are studied by means of the  $H$ -invariant abelian functions on  $A_{-1}$ .

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