



ASPECTS OF LUSTERNIK-SCHNIRELMANN CATEGORY

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Abstract. In this paper we review certain Lusternik-Schnirelmann categorical notions that pertain especially to Eilenberg-Mac Lane spaces. Further, we introduce a new categorical invariant that allows a refined estimate for category. Finally, we mention some results about topological complexity and relate these to category.

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