

LIQUID DROPS, SOAP BUBBLES AND SURFACES WITH CONSTANT MEAN CURVATURE

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Abstract. This is a review of the theory of compact surfaces with constant mean curvature with special attention on surfaces with non empty boundary. We analyze the relation between the geometry of the boundary curve with the one of the surface that spans. This will allow to give a mathematical support to describe the geometry of liquid drops and soap bubbles.

MSC: 53A10

Keywords: Dirichlet problem, mean curvature, soap bubble, tangency principle

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